

Chapter 6: FACTORING & APPLICATIONS

6.1 The Greatest Common Factor; Factor by Grouping

FACTORING

(to express as a multiplication)

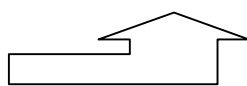
Step 1: Factor out GCF (greatest common factor)

Step 2: Count the terms

4-terms \implies grouping (2-steps)

3-terms \implies trial & error or master product

2-terms \implies difference of squares

1. $\underbrace{a^2}_a - \underbrace{b^2}_b$ then factor as $(a + b)(a - b)$
a & b are the roots used in  a sum & difference

difference of cubes

2. $\underbrace{a^3}_a - \underbrace{b^3}_b$ then factor as $(a - b)(a^2 + ab + b^2)$

sum of cubes

3. $\underbrace{a^3}_a + \underbrace{b^3}_b$ then factor as $(a + b)(a^2 - ab + b^2)$

FACTOR (verb): express as a multiplication

example: Factor 12

$$12 = 1(12)$$

$$12 = 2(6)$$

$$12 = 3(4)$$

note: $12 = (1) + (11)$

 Not factored

note: factors of a number divide it evenly, 1,2,3,4,12 divide 12 evenly

$$12 = 2(2)(3) = 2^2(3) \text{ this is called the Prime Factorization of 12}$$

because all the factors are prime numbers

Greatest Common Factor (GCF)

example: Find the GCF of 12 and 16.....do you know the answer??

If not...step 1: prime factor each number (tree method or division)

$$12 = 2^2 (3)$$

$$16 = 2^4$$

step 2: multiply the factors they have in common

$$\text{GCF} = 2^2 \text{ or } 4 \quad \text{note: since 4 is a factor (GCF) it will divide 12 \& 16 evenly}$$

example: Find the GCF of $21m^7$, $-18m^6$, $45m^8$

$$\begin{aligned} \text{step 1:} \quad 21m^7 &= 3 \cdot 7 \cdot m^7 \\ -18m^6 &= (-1) \cdot 2 \cdot 3^2 \cdot m^6 \\ 45m^8 &= 3^2 \cdot 5 \cdot m^8 \end{aligned}$$

$$\text{step 2:} \quad \text{GCF} = 3m^6$$

FACTORING

Step 1: Factor out GCF or Divide out GCF

example: $21m^7 - 18m^6 + 45m^8$ remember $\text{GCF} = 3m^6$ (see above)
 $(3m^6)(7m - 6 + 15m^2)$ check this answer by multiplying out and seeing if you get the original problem

FACTORING

Step 1: Factor out GCF

Step 2: Count the terms

4-terms: grouping (2-steps)

example 1:

$$\begin{array}{l} \underbrace{2x + 6} + \underbrace{ax + 3a} \\ 2(x + 3) + a(x + 3) \end{array}$$

four terms, no GCF, we try groups of 2

factor out GCF of each group
notice there is now a GCF of $(x + 3)$


$$(x + 3)(2 + a)$$

SO factor out $(x + 3)$, now the expression is completely factored

Look at the original addition problem, it has now been rewritten as a multiplication problem...factored!!

example 2:

$$\begin{array}{l} \underbrace{6xy - 21x} - \underbrace{8y + 28} \\ 3x(2y - 7) - 4(2y - 7) \end{array}$$

 note sign change because you are factoring out a **negative** number (-4)

$$(2y - 7)(3x - 4)$$

The sign change in example 2 is often overlooked on the exam. Also remember when factoring by grouping you are done until you've completed 2 steps.